

# Streamwise distribution of the recovery factor and the local heat transfer coefficient to an impinging circular air jet

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**Abstract**—An investigation of the radial distribution of the recovery factor and the local heat transfer for an axisymmetric impinging air jet formed by a smooth nozzle is described. The recovery factor is dependent on the jet nozzle to impingement plate spacing, but is independent of jet Reynolds number. The maximum stagnation region heat transfer occurs at a nozzle to impingement plate spacing of about eight jet diameters. A correlation is obtained for the average heat transfer from the surface.

## 1. INTRODUCTION

IN MANY industrial systems—including high temperature gas turbines, paper and glass manufacturing plants and high density electrical and electronic equipment—impinging jets of fluid, usually air, are used to cool, heat or dry a surface. Over the past three decades numerous studies have been reported on the heat transfer to impinging single and multiple jets. Table 1 lists investigations [1–25] which considered a single impinging circular jet. A survey of early works is provided by Martin [26].

Gardon and Cobonpue [3] first described the rate of heat transfer to an impinging jet as proportional to the difference between the (impingement) plate temperature and the adiabatic wall temperature, which varies from point to point on the impingement surface. In refs. [11, 13, 21] adiabatic wall temperature is used in calculating the heat transfer coefficient with an impinging single round jet in the presence of a cross-flowing air stream. Hollworth and Wilson [23] report measurements of effectiveness (essentially recovery factor—dimensionless adiabatic wall temperature) with an impinging circular air jet. In the same experimental apparatus Hollworth and Gero [24] investigated local heat transfer. Obot *et al.* [19] studied the effect of jet-exit geometry on impingement heat transfer. They found the jet-exit geometry mainly influences the heat transfer coefficient in the stagnation region for  $L/D < 6$ .

In the present investigation, adiabatic wall temperature and local heat transfer from an impinging plate to a circular air jet are measured for jet to impingement plate spacings ( $L/D$ ) of 2, 4, 5, 6, 7, 8, 10 and 12, with nominal jet Reynolds numbers of 61 000, 79 000, 89 000, 106 000 and 124 000.

## 2. EXPERIMENTAL APPARATUS AND OPERATIONAL PROCEDURE

The experimental apparatus is similar to those described in refs. [11, 13, 21]; only a brief description of it is given here. The heat transfer test plate is 24.05 cm wide and 114 cm long. Air for the jet is supplied by the building compressor. After filtering and regulation, the air is metered by a replaceable thin-plate orifice. In a 127-cm-long section, an electric heater helps control the desired (total) air temperature, usually close to the ambient room air temperature. Next, the air is introduced into an insulated delivery tube 4.09 cm I.D. and 83 cm long. Attached to this tube is the jet exit assembly.

The jet exit assembly, Fig. 1a, consists of an upper bracket, a spacer and a nozzle. The upper bracket is fastened to the delivery pipe from above and a 2.54 cm thick piece of plexiglas support from below. Brass spacers of different lengths are used to vary the jet nozzle to impingement-plate spacing. The spacer is threaded into the upper bracket. The quarter-ellipse aluminum jet nozzle is designed according to the ASME power code [27]. The impingement plate is made of thin textolite with styrofoam backing (Fig. 1b). Twenty-one stainless-steel heating foils (0.0254 mm thick) are bonded on the textolite, and 63 36-gauge iron-constantan thermocouples are embedded in the test plate in thermal contact with the stainless-steel heating foils via copper oxide.

In each test run, the mass flow is adjusted to give the desired Reynolds number and the air is heated so that:

$$T_j^\circ \approx T_R.$$

Each test run is composed of two parts. First, the temperature distribution on the test plate is measured when the wall-heat flux is zero. This provides the adiabatic wall temperature  $T_{aw}$ . Then, the wall temperature distribution is measured on the test plate

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**NOMENCLATURE**

$A_j$  jet exit area  
 $c_p$  specific heat of fluid  
 $D$  jet diameter (1.27 cm)  
 $h$  local heat transfer coefficient,  $q/(T_w - T_{aw})$   
 $\bar{h}_q$  area average heat transfer coefficient for constant heat flux wall,  $q/(T_w - T_{aw})$   
 $j$  exponent in equation (4)  
 $k$  thermal conductivity of fluid  
 $L$  jet to impingement plate spacing  
 $\dot{m}_j$  jet mass flow rate  
 $Nu$  local Nusselt number,  $hD/k$   
 $\bar{Nu}$  Nusselt number averaged over area from  $R = 0$  to  $R = R_i$  [equation (4)]  
 $\bar{Nu}_q$  area averaged Nusselt number for constant heat flux [equation (7)]  
 $q$  wall heat flux

$Re$  jet Reynolds number,  $\bar{U}_j D / \nu_j$   
 $r$  recovery factor,  $(T_{aw} - T_j^s) / [\bar{U}_j^2 / (2c_p)]$   
 $R$  radial distance from geometrical center of jet—shown as greater or less than zero on the measurement line  
 $T_{aw}$  adiabatic wall temperature  
 $T_j^s$  jet static temperature  
 $T_j^\circ$  jet total temperature, measured 127 mm upstream of the jet exit  
 $T_R$  room temperature  
 $T_w$  wall temperature  
 $\bar{U}_j$  jet velocity,  $\dot{m}_j / \rho_j A_j$

**Greek symbols**

$\nu$  kinematic viscosity  
 $\rho_j$  fluid density at jet exit.

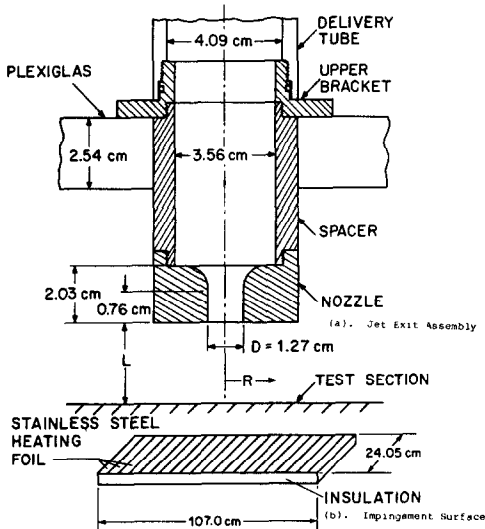


FIG. 1. Jet nozzle and test plate.

where  $q$  is the heat flux from the surface corrected for lateral conduction, for conduction to the back and for radiation. The definition of local heat transfer coefficient [equation (2)], based on the difference between the wall temperature and the adiabatic wall temperature, is well established [3, 11, 13, 21, 24]. Knowledge of  $T_{aw}$  is of great importance if meaningful results are to be obtained that can be used in different applications.

The adiabatic wall temperature measurements are presented in dimensionless form using a recovery factor

$$r = \frac{T_{aw} - T_j^s}{\bar{U}_j^2 / 2c_p} \quad (3)$$

Figures 2 and 3 show the radial variation of the recovery factor for jet to impingement plate spacings ( $L/D$ ) of 2 and 8, respectively. Although care was taken to set  $T_j^\circ$  equal to the room temperature,  $T_R$ , by heating the jet air, small variations in temperature with time produced some scatter in  $r$  at low jet Reynolds number. Figures 2 and 3 each contain four graphs

after the current is turned on in the heating foils. Approximately 1.5 h are required to reach steady-state conditions for each part of the test run.

**3. RESULTS**

Experimental results for heat transfer are presented in terms of the Nusselt number

$$Nu = \frac{hD}{k} \quad (1)$$

The local heat transfer coefficient is defined by

$$h = \frac{q}{T_w - T_{aw}} \quad (2)$$

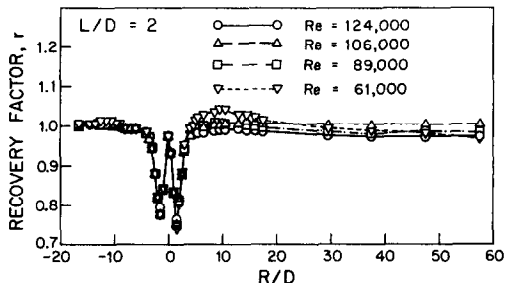


FIG. 2. Radial distribution of the recovery factor for  $L/D = 2$ .

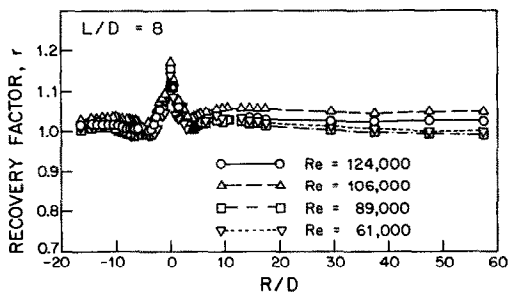


FIG. 3. Radial distribution of the recovery factor for  $L/D = 8$ .

corresponding to the different Reynolds numbers. Inspection of these figures and results for the other values of  $L/D$  show that the recovery factor is independent of Reynolds number. Figure 4 presents radial distributions of the recovery factor for a number of different spacings at  $Re = 124\,000$ . Note that  $r$  is dependent on spacing.

Figure 5 shows recovery factor as a function of  $L/D$  for various  $Re$  at  $R/D = 0$  and 2. At the stagnation point ( $R = 0$ ), for all  $Re$  the recovery factor is close to unity at  $L/D = 2$ , increases till  $L/D \approx 8$ , and then levels off at larger spacings. For  $R/D = 2$ , close to the minima\* shown in Fig. 2, the recovery factor is also essentially independent of  $Re$  but varies significantly with spacing. The increase in recovery factor with  $L/D$  is attributed to greater mixing of warmer ambient air (the jet static temperature is reduced below the ambient temperature by the dynamic temperature) with the jet as  $L/D$  increases.

Turning our attention back to Figs. 2-4, outside the region near stagnation (for  $R/D \geq 4$ ),  $r$  is close to unity. Local minima appear near the stagnation point at  $R/D \approx \pm 2$ . These local minima have their lowest value at  $L/D \approx 2$ . The occurrence of significant local minima in  $r$  at small  $L/D$  can be attributed to energy separation in the highly curved flow present. At small spacing where the impingement plate would be within the potential core of the jet, the jet is surrounded by vortex rings in the shear layer. These vortex rings keep their orderly structure after impingement [28]. For vortex motion, as discussed by Hartnett and Eckert [29], an energy separation exists where the minimum energy occurs at the center of the vortex. This corresponds to the local minimum in recovery factor at  $R/D \approx 2$ . At  $L/D > 4$ , breakdown of the vortex rings takes place [28] and the local minimum of  $r$  tends to disappear (cf. Fig. 4).

The heat transfer results are represented in dimensionless form by the Nusselt number. In general, the local Nusselt number would be a function of  $L/D$ ,  $R/D$ ,  $Pr$  (approximately constant in the present study)

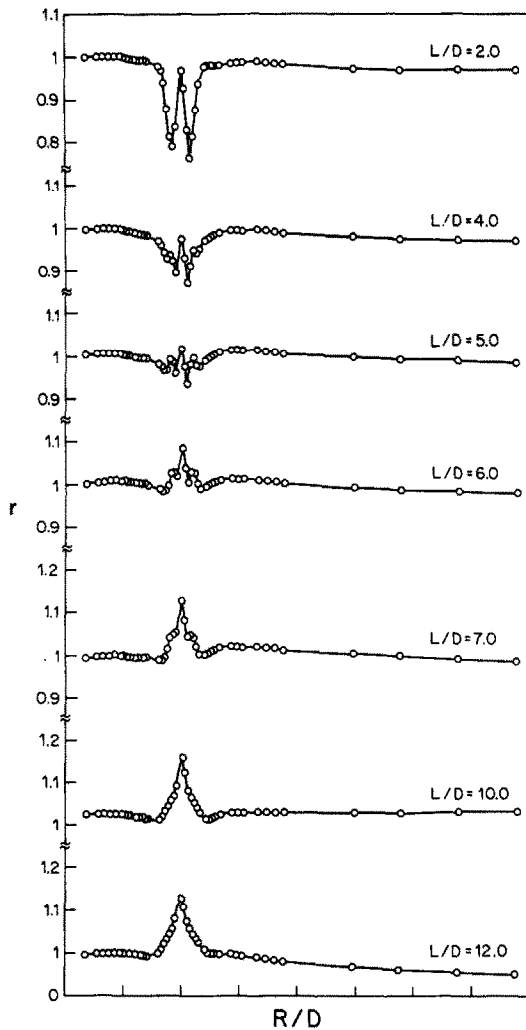


FIG. 4. Radial distribution of the recovery factor at different jet to plate spacings,  $Re \approx 124\,000$ .

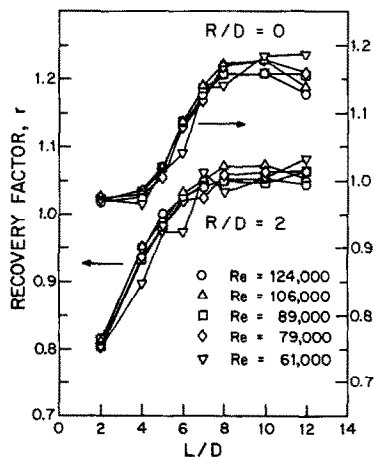


FIG. 5. Variation of the recovery factor with jet to impingement plate spacing at  $R/D = 0$  and 2.0.

\* As measurements were taken along a line through the stagnation point on the plate, values of  $R$  greater and less than zero are plotted. Since the jet is axisymmetric this is not strictly necessary. The minima discussed at  $R/D \approx \pm 2$  are really one off-center minimum.

Table I.

Ref.	Author(s)	Geometry	$D$ (cm)	$Re_j = U_j D / \nu$	$L/D$	Type of measurements	Fluid outlet
1	Perry	long nozzle, length not known at angles	1.65, 2.16	$7 \times 10^3$ – $30 \times 10^3$ , for $D = 1.65$	$\geq 8$	area average	hot air in all directions
2	Vikers	short tube, length not known	not known	250–950	$8 \leq L/D \leq 20$	local	air into a circular box in all directions
3	Gardon and Cobonpue	well rounded inlet and short throat, length not known	0.23–0.9	$7 \times 10^3$ – $1.12 \times 10^5$	$\geq 0.5$	local	air in all directions
4	Smirnov <i>et al.</i>	long tube, length = $80D$	0.25, 0.64, 1.07, 2.13, 3.0, 3.66	$50$ – $31 \times 10^3$	$0.5 < L/D < 10$	averaged	water in all directions
5	Huang	orifice thickness = $0.317D$	0.317, 0.635	$10^3$ – $10^4$	1.25–10	averaged (2.5 cm) around-stagnation	hot air in all directions
6	Schlunder and Grzelinski	long tube, length not known	2.5	$34 \times 10^3$ – $124 \times 10^3$	1.25–10	local mass transfer	air in all directions
7	Nakatogawa <i>et al.</i>	nozzle	0.8	area average velocity = $35$ – $321 \text{ m s}^{-1}$	0.5–24	around stagnation	all directions
8	Kataoka and Mizushima	convergent nozzle	1	2970, 5030, 9800	5.86, 8.21	mass transfer	electrochemical technique
9	Donaldson and Snedeker	convergent nozzle	1.29	based on half radius	7, 10, 15, 20, 20	mass transfer	air in all directions
10	Den Ouden and Hogendoorn	nozzle	1.3–5.7	$0.38 \times 10^3$ – $2.64 \times 10^5$	1–6	local around stagnation	air in all directions
11	Bouchez and Goldstein	orifice $L/D = 12$ , tube $L/D = 6$	1.27	$35 \times 10^3$ – $125 \times 10^3$	6, 12	local	air impingement in a well-defined crossflow

12	Hollworth and Bowley	nozzle $10D$ long, orifice $1/D$ long	0.318–1.27	$2.5 \times 10^4$ $1.9 \times 10^5$	3.5–14	local	air impingement in a well-defined crossflow
13	Sparrow <i>et al.</i>	orifice for $L/D = 12$ or various lengths for $3 \leq L/D \leq 12$	1.27	$35 \times 10^3$ $125 \times 10^3$	3, 4, 5, 6, 8, 10, 12	local	air impingement in a well-defined crossflow
14	Hoogendoorn	long tube and nozzle with smooth contraction	5.7	$2 \times 10^4$ $9 \times 10^4$	2–10	local liquid crystal	air in all directions
15	Kataoka <i>et al.</i>	nozzle smooth contraction	2.8	$4 \times 10^3$ $15 \times 10^3$	2–10	local mass transfer	electrochemical technique
16	Yokobori and Hirata	nozzle	4.0	$10^3$ $67 \times 10^3$	2–12	local around stagnation	water flow visualization
17	Popiel <i>et al.</i>	exit of tunnel burner	1.38	1860–1050	2–20	local heat flux meter	combustion products in all directions
18	Sparrow and Lovell	orifice at angles $90^\circ$ – $30^\circ$	0.635	$2.5 \times 10^3$ $10^4$	7, 10, 15	local mass transfer (naphthalene)	air in all directions
19	Obot <i>et al.</i>	orifice of various thicknesses and rounded nozzle of various lengths not clear exp. and num.	1.905	$15 \times 10^3$ $60 \times 10^3$	2–12	local	air in all directions
20	Amano and Jensen	nozzle of various lengths not clear exp. and num.	0.46	$10^4$ – $2 \times 10^4$ $4 \times 10^4$	4, 7, 10	local	air in all directions inside large enclosure
21	Goldstein and Behbahani	orifice, $L/D = 12$ , tube $L/D = 6$	1.27	$25 \times 10^3$ $124 \times 10^3$	6, 12	local	air with and without crossflow
22	Goldstein and Timmers	orifice thickness = $D$	1.00	$40 \times 10^3$	2, 6	local (liquid crystals)	air in all directions
23	Hollworth and Wilson	orifice thickness = $D$	0.25, 1.0	$7 \times 10^3$ $7 \times 10^4$	1, 5, 10, 15	local	air in all directions
24	Hollworth and Gero	orifice thickness = $D$	0.25, 1.0	$5 \times 10^3$ $6 \times 10^4$	1, 5, 10, 15	local	air in all directions
25	Hrycak	orifice at the end of a tube	0.318–1.27	$1.4 \times 10^3$ $6 \times 10^4$	1–14	average over area of 5 mm diameter	air in all directions
	Present study	orifice	1.27	$61 \times 10^3$ $12 \times 10^4$	2–12	local	air in all directions

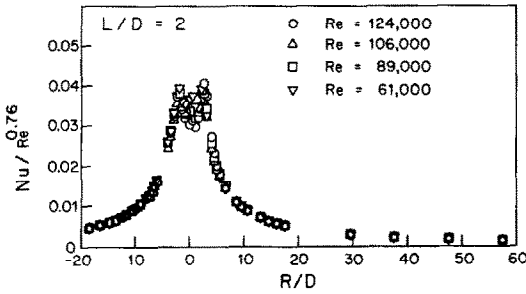


FIG. 6. Radial distribution of  $Nu/Re^{0.76}$  for  $L/D = 2$ .

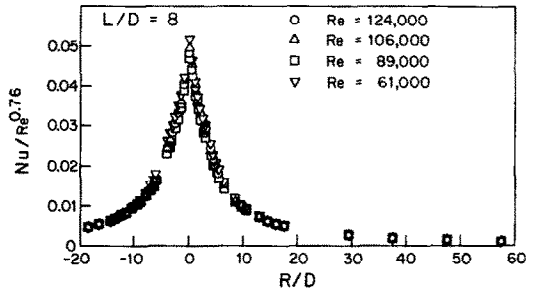


FIG. 8. Radial distribution of  $Nu/Re^{0.76}$  for  $L/D = 8$ .

and  $Re$ . The dependence on  $Re$  can be approximated by a power-law dependence

$$Nu \propto Re^j \tag{4}$$

The value of  $j$  is somewhat dependent on  $R/D$ . Close to the stagnation point  $j$  is smaller ( $\sim 0.5$  for small  $L/D$ ) than at larger  $R$ . For a plane wall jet, values of 0.75(30) and 0.80(31) have been found. For convenience, a constant value of  $j$  is used in the present correlation (cf. discussion on correlation below).

Figures 6–9 contain plots of  $Nu/Re^{0.76}$  as a function of radial position for jet to impingement plate spacings ( $L/D$ ) of 2, 5, 8 and 10 respectively. On each figure, results for  $Re = 61\,000$ ,  $89\,000$ ,  $106\,000$  and  $124\,000$  are presented. As can be seen from these figures,  $Nu/Re^{0.76}$  is essentially independent of  $Re$  for all  $L/D$  in the range of the present experiments except close to  $R = 0$ .  $Nu/Re^{0.76}$  has little dependence on  $L/D$  as well as  $Re$  in regions for which  $|R/D| \geq 4$ . At these large radii  $Nu$  decreases as a result of the increase in the boundary thickness.

In the stagnation region,  $Nu$  varies with spacing. At small spacing ( $L/D = 2, 4$  and  $5$ ), secondary maxima appear at  $R/D \approx \pm 2$ . For  $L/D = 2$ , these local maxima are higher than the stagnation ( $R/D = 0$ ) values of  $Nu$  (Fig. 6). This can also be observed in Fig. 10, where  $Nu/Re^{0.76}$  is shown as a function of  $L/D$  for the different  $Re$  at  $R/D = 0$  and  $2$ . The local maxima at  $R/D \approx 2$  are attributed to the enhancement of heat transfer from entrainment caused by vortex rings in the shear layer. Local maxima in  $Nu$  were also observed by other investigators [3, 14, 22]. The stagnation  $Nu$

increases with  $L/D$  and reaches its maximum at  $L/D = 8$ , beyond which it decreases (cf. Fig. 10). This increase in stagnation  $Nu$  can be related to penetration of turbulent-induced mixing from the shear layer. The decrease beyond  $L/D = 8$  is a consequence of lower arrival velocity of the jet. Note again there is little effect of spacing on  $Nu$  for  $R/D > 4$  in the range of the present tests.

As the jet is axisymmetric, the radial distribution of  $Nu$  can be averaged to give the mean Nusselt number

$$\bar{Nu} = \frac{2}{R^2} \int_0^R Nu R dR \tag{5}$$

The integral is determined numerically for  $R/D = 0.5, 1, 2, 3, 6, 18$  and  $32$  for  $L/D \geq 6$ . These results are satisfactorily correlated by:

$$\frac{\bar{Nu}}{Re^{0.76}} = \frac{(A - |L/D - 7.75|)}{B + C(R/D)^n} \tag{6}$$

where  $A = 24, B = 533, C = 44$  and  $n = 1.285$ . Figure 11 shows this correlation; the spread in the data is indicated by the vertical bars.

Equation (5) evaluates  $\bar{Nu}$  based on the assumption of constant  $(T_w - T_{aw})$  over the impingement surface. In this study, however, heat flux at the wall is constant. Defining an average temperature difference

$$\overline{T_w - T_{aw}} = \frac{2}{R^2} \int_0^R (T_w - T_{aw}) R dR \tag{7}$$

and

$$\bar{h}_q = q / (\overline{T_w - T_{aw}}) \tag{8}$$

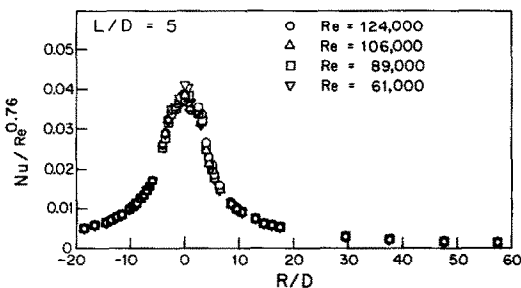


FIG. 7. Radial distribution of  $Nu/Re^{0.76}$  for  $L/D = 5$ .

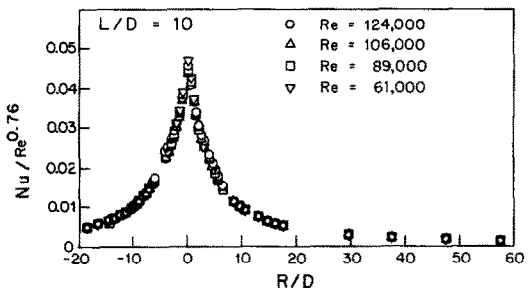


FIG. 9. Radial distribution of  $Nu/Re^{0.76}$  for  $L/D = 10$ .

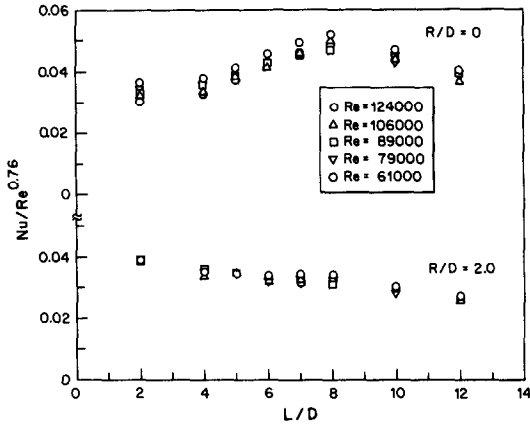


FIG. 10. Variation of  $Nu/Re^{0.76}$  with jet to impingement plate spacing at  $R/D = 0$  and  $2.0$ .

the area-averaged Nusselt number based on the constant heat flux becomes :

$$\overline{Nu}_q = \frac{R^2}{2} \left/ \int_0^R \frac{1}{Nu} R dR \right. \quad (9)$$

A correlation similar to equation (6) can be obtained to describe  $\overline{Nu}_q$

$$\frac{\overline{Nu}_q}{Re^{0.76}} = \frac{(A - |L/D - 7.75|)}{B + C(R/D)^m} \quad (10)$$

where  $A$ ,  $B$  and  $C$  are as given for equation (6) above and  $m = 1.394$ . The range of validity is the same as for equation (6).  $\overline{Nu}_q$  is found to be closely equal to  $\overline{Nu}$  (cf. Fig. 11) up to  $R/D = 4$ . At larger  $R/D$ ,  $\overline{Nu}_q$  is somewhat higher than  $\overline{Nu}$ .

The exponent, 0.76, for equations (4) and (10) is chosen from a least-squares analysis to minimize the standard deviation of the data from the correlation. The variation of the standard deviation with the value of the exponent is small in the region of the minimum, and other values could be used. If 0.75 or 0.8 were used for  $j$ , equations (6) and (9) would be little changed other than  $A = 475$  and  $B = 39$  when  $j = 0.75$  and  $A = 842$  and  $B = 70$  when  $j = 0.8$ . These variations in the correlation have some merit when comparing the

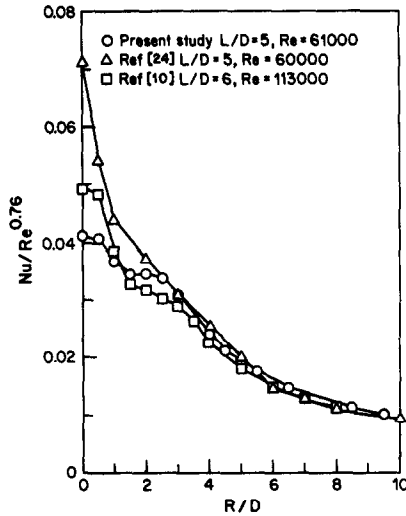


FIG. 12. Comparison of the local heat transfer results with other studies.

results to analytical predictions particularly in the wall jet region at large  $R$ .

*Comparison of results*

Local heat transfer results are compared in Fig. 12 with results from earlier investigations. Inspection of Fig. 12 shows good agreement between the present study and those of refs. [10, 24] for  $R/D > 2$ . However, considerable differences in heat transfer coefficients exist in the stagnation region ( $R/D < 2$ ). This discrepancy can be attributed [19], at least partly, to differences in the jet-exit geometries of the different studies. Area averaged heat transfer coefficients are compared in Table 2 with the correlation in ref. [26] using results of various investigators. Good agreement is observed.

**4. SUMMARY AND CONCLUDING REMARKS**

The recovery factor on the impingement surface is independent of jet Reynolds numbers, but is dependent on jet to impingement plate spacing. At small

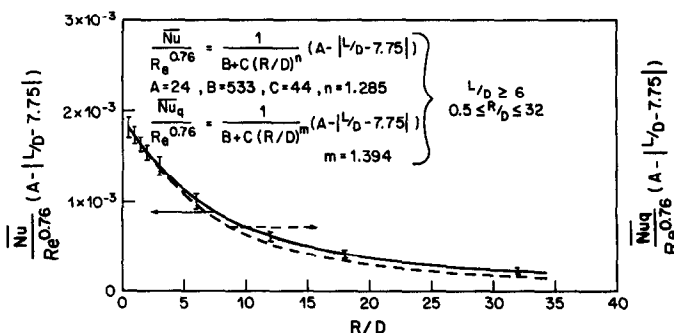


FIG. 11. Area-averaged heat transfer correlation for constant surface heat flux and constant surface temperature.

Table 2. Comparison of area-averaged Nusselt number

$R/D$	$L/D$	$Re = 61\,000$		$Re = 89\,000$		$Re = 12\,400$	
		Ref. [26]	Present study $\overline{Nu}_q$	Ref. [26]	Present study $\overline{Nu}_q$	Ref. [26]	Present study $\overline{Nu}_q$
3	6	159	151	207	202	261	260
	8	149	162	194	216	245	278
	12	133	134	172	179	218	231
6	6	103	126	133	168	168	217
	8	99	134	129	180	163	232
	12	93	112	121	150	153	193

spacing, the recovery factor in the stagnation region has a minimum near  $R/D \approx 2$  apparently due to energy separation in the vortex ring region in the shear layer. For  $L/D$  greater than about 5 up to the largest spacing studied ( $L/D = 12$ ), the stagnation region recovery factor can be greater than unity due to mixing of the ambient fluid with the jet. The heat transfer is best correlated by  $Nu/Re^{0.76}$  for all  $L/D$ . The Nusselt number has a maximum at  $R/D \approx 2$  for jet-to-plate spacings up to  $L/D = 5$ . The maximum stagnation Nusselt number occurs at about  $L/D = 8$ .

*Acknowledgement*—The research was supported by a grant from the Engineering Research Program of the Office of Basic Energy Science, U.S. Department of Energy.

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#### DISTRIBUTION DU FACTEUR DE RECUPERATION ET DU COEFFICIENT LOCAL DE CONVECTION POUR UN JET D'AIR CIRCULAIRE IMPACTANT

**Résumé**—On décrit une étude de la distribution radiale du facteur de récupération et du coefficient de convection local pour un jet axisymétrique d'air qui sort d'une tuyère lisse et qui frappe une surface. Le facteur de récupération dépend de la distance entre la sortie du jet et la plaque, mais il est indépendant du nombre de Reynolds. Le maximum du transfert thermique au point d'arrêt est obtenu à une distance de huit diamètres. Une formule est donnée pour le transfert thermique global sur la surface.

#### VERTEILUNG DES 'RECOVERY'-FAKTORS UND DES ÖRTLICHEN WÄRMEÜBERGANGSKOEFFIZIENTEN BEIM AUFSTREIFEN EINES LUFTSTRAHLES MIT KREISQUERSCHNITT

**Zusammenfassung**—Beschrieben wird eine Untersuchung der radialen Verteilung des 'Recovery'-Faktors und des örtlichen Wärmeübergangskoeffizienten beim Auftreffen eines axialsymmetrischen Luftstrahles, der durch eine gut gerundete Düse erzeugt wird. Der 'Recovery'-Faktor ist abhängig vom Abstand zwischen der Düse und der angeströmten Platte, jedoch unabhängig von der Reynoldszahl des Strahles. Der maximale Wärmeübergangskoeffizient im Staugebiet ergibt sich, wenn der Düsenabstand dem achtfachen Strahldurchmesser entspricht. Es wurde eine Beziehung für den mittleren Wärmeübergangskoeffizienten an der Oberfläche ermittelt.

#### РАСПРЕДЕЛЕНИЕ В РАДИАЛЬНОМ НАПРАВЛЕНИИ КОЭФФИЦИЕНТОВ ВОССТАНОВЛЕНИЯ И ЛОКАЛЬНОГО ТЕПЛОПЕРЕНОСА К КРУГЛОЙ ВОЗДУШНОЙ СТРУЕ, НАТЕКАЮЩЕЙ НА ПРЕГРАДУ

**Аннотация**—Описываются результаты исследования радиального распределения коэффициента восстановления и локального теплопереноса для осесимметричной набегающей струи воздуха, истекающей из гладкого сопла. Показано, что коэффициент восстановления зависит от отношения расстояния до пластины к диаметру сопла, но независим от числа Рейнольдса струи. Максимальная застойная область теплообмена имеет место при указанном геометрическом соотношении, равном 8. Получена зависимость для осредненного теплопереноса с поверхности.